# Richer and Busier? The Facts, Causes, and Consequences of Labor Supply in China 

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## Motivation

- Final consumption is a composite of consumption good and time (Becker, 1965). As we become richer, how do we change the ways of allocating our time?
- Existing evidence.
- Hours fall steadily in advanced economies in the past 150 years (Boppart and Krusell, 2020).
- High-income countries work less than low-income countries (Bick et al., 2018).

Three-hour shifts or a fifteen-hour week may put off the problem for a great while. For three hours a day is quite enough to satisfy the old Adam in most of us!

John Maynard Keynes, 1930
Economic Possibilities for our Grandchildren

## Motivation

- Much less is known about China's secular trend in hours and leisure, after 40 years of rapid growth.


I personally think that 996 is a huge blessing. How do you achieve the success you want without paying extra effort and time?

Jack Ma, 2019
In an interview as CEO of Alibaba

Figure: Market Hours Per Worker Across Countries

Notes: This figure plots the sequences of the average annual market hours per worker corresponding to the logarithm of GDP per capita in different countries. Data source: Penn World Table 10.0, and National Bureau of Statistics (China).

## This Paper Studies The Secular Trend in Time Allocation Within China

- Do Chinese work for longer hours as China becomes richer? Who work for longer hours?
- How about non-market hours and leisure?
- What drives these changing patterns in time allocation?


## Preview of Findings

Utilize Chinese Time Use Survey 2008 and 2018, China Family Panel Studies 2010-2020,

- The secular trend in time allocation among Chinese.
- Urban: market hours $\uparrow$ (3-6 hours a week), home production $\downarrow$, child care $\uparrow$, leisure $\downarrow$.
- Rural: market hours $\downarrow$, home production $\downarrow$, child care $\uparrow$, leisure $\uparrow$.
- Among wage workers, from 2010 to 2020:
- a rise in both wage rate $(\sim 60 \%)$ and market hours ( $\sim 6 \%$ )
- At any given time, Corr(market hours, wage rate) $<0$
- 



- A quantitative heterogeneous agent model: life cycle, incomplete market, home production, Pay-as-you-go pension system.
- TFP growth $\rightarrow$ market hours $\downarrow$; non market hours $\downarrow \downarrow$
- Capital augmenting productivity growth in home production $\rightarrow$ market hours $\uparrow$; non market hours $\downarrow$
- Rising income uncertainty and change in demographics structure $\rightarrow$ market and non market hours $\uparrow$
- Successfully recover trend in market hours, non market hours and correlation between market hours and wage rate.

Data

## Data

- Chinese Time Use Survey 2008 and 2018.
- Conducted by the National Bureau of Statistics in May 2008 and April 2018, repeated cross-section.
- National representative: 37,000 individuals in 2008, 48,000 individuals in 2018 from 10 provinces.
- Advantage: Based on 24-h diaries, detailed time-use categories: market hours, home production, child care, education, and leisure.
- China Family Panel Studies 2010-2020.
- Carried out by Peking University every two years.
- Nationwide representative and longitudinal household survey, around 30,000 adults each round.
- Advantage: can estimate income process, focus on employees who report working hours, labor income.


## Empirical Facts

## Hours Per Person

Table: Time Allocation by Area and Gender

|  | $\begin{aligned} & \text { All } \\ & \text { male } \end{aligned}$ |  | All female |  | Urban male |  | Urban female |  | Rural male |  | Rural female |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 |
| Market hours | 42.0 | 43.3 | 30.7 | 30.6 | 33.0 | 39.6 | 25.0 | 27.9 | 51.7 | 47.7 | 37.3 | 33.1 |
| Non-market hours |  |  |  |  |  |  |  |  |  |  |  |  |
| Home production | 8.9 | 7.2 | 23.1 | 18.2 | 10.7 | 7.4 | 23.6 | 17.3 | 6.9 | 7.1 | 22.5 | 19.2 |
| Child care | 1.7 | 2.8 | 4.2 | 8.3 | 2.1 | 4.0 | 4.0 | 8.7 | 1.2 | 1.6 | 4.4 | 7.9 |
| Education | 4.0 | 4.0 | 3.6 | 3.9 | 4.7 | 4.7 | 4.2 | 4.3 | 3.2 | 3.4 | 3.0 | 3.4 |
| Leisure | 111.4 | 110.7 | 106.4 | 107.0 | 117.0 | 112.8 | 111.2 | 109.8 | 105.0 | 108.2 | 100.8 | 104.4 |
| Total | 168 | 168 | 168 | 168 | 168 | 168 | 168 | 168 | 168 | 168 | 168 | 168 |

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Notes: This table reports the average weekly hours spent on each broad-use category of activities. The rural-urban definition is based on where the individual lives at the time of the survey. The sample includes all individuals at ages 15-74. All means are calculated using fixed demographic weights: 12 age groups $\times 6$ education groups Data source: Chinese Time Use Survey 2008 and 2018.

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## Extensive vs. Intensive Margin

Table: Employment Rate and Hours Per Worker

|  | All male |  | All female |  | Urban male |  | Urban female |  | Rural male |  | Rural female |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 | 2008 | 2018 |
| Employment rate, \% | 79.3 | 78.8 | 67.7 | 63.3 | 69.5 | 71.6 | 55.3 | 54.4 | 89.9 | 86.6 | 82.0 | 75.5 |
| Market hours per worker | 49.9 | 50.8 | 40.9 | 40.7 | 43.0 | 48.6 | 39.0 | 42.7 | 55.6 | 50.9 | 42.4 | 38.8 |

Notes: This table reports the average weekly hours spent on each broad-use category of activities. The rural-urban definition is based on where the individual lives at the time of the survey. The sample includes all individuals at ages 15-74.
Data source: Chinese Time Use Survey 2008 and 2018.

- Urban: mainly driven by intensive margin
- Rural: driven by both intensive and extensive margin

The main puzzle is for urban area, intensive margin. From now on, We mainly focus on wage workers.

## Market Hours Using CFPS: Heterogeneity and Composition



## Increasing Working Hours Coincide With Growing Wages



Hours Per Worker


Wage Rate

Figure: Hours Per Worker and Wage Rate, 2010-2020

## Substitution Effect Dominates? Probably No

What is the puzzle?

- Cross sections: market hours and wage rates are negatively correlated
- Over time: An increase in market hours is associated with an increase in wage rate


Male Sample


Female Sample

Figure: Correlation of Hour and Wages: 2010 vs. 2020

# Why Market Hours Still Increase While Wages Grow? 

## Substituting Non-Market Hours with Market Hours



Share of Online Takeout in Catering Industry


Numbers of Washing Machine Per 100 hhs.

- Market goods substitute for home goods
- Home capital substitutes for non market hours


## Rising Wage Inequality and Uncertainty



Wage Rate Growth By Wage Rate Percentile


Variance of Log (Wage) over Time

Figure: Wage Inequality Between 2010 and 2020

Decompose the rise in wage inequality into initial dispersion, variance of persistent shocks and variance of transitory shocks.

## Aging and Replacement Ratio



Death Rate


Birth Rate

Figure: Age-specific Death Rate and Birth Rate

Model

## Preliminaries

A model speak to (urban)wage workers with no extensive margin. An extension of Huggett (1996) with home production. Following (Heathcote et al., 2010).

- Time is discrete and infinite. No aggregate uncertainty.
- The economy is populated by a continuum of overlapping generation individuals with age $j$, $j \in \mathcal{J} \equiv\{1,2, \ldots, J\}$.
- Individuals live a maximum of $J$ periods and face an probability $s_{j}$ of surviving up to $j$ conditional on surviving up to $j-1$. Population is growing at an exogenous rate $n$. Let $\mu_{j}$ be the density of population with age $j$ :

$$
\mu_{j}=\frac{s_{j}}{1+n} \mu_{j-1}
$$

- Individuals enter into labor market at age $j=1$ and work for $J^{w}$ periods. They retire from $J^{w}+1$ starting receive pension and die with probability of 1 at age $j=J$.


## Production

Final good is produced by a representative firm who use aggregate capital $K$ and aggregate market labor as inputs $H$ with Cobb-Douglas technology:

$$
Y=A K^{\alpha} H^{1-\alpha}
$$

- Final good can be used for market goods consumption, investment and government expenditure.
- We normalize the price of final good to be one.

Final good can also be used to produce home capital $K_{h}$ according to a linear technology:

$$
K_{h}=A_{h} Y_{h}
$$

where $Y_{h}$ is the market good input and $A_{h}$ is the productivity in producing home capital. We assume the depreciation rate of home capital is 1 .

## Preferences

The period utility function is:

$$
u(c, h)=\frac{c^{1-\gamma}}{1-\gamma}-\psi \frac{h^{1+\sigma}}{1+\sigma}
$$

where $c \geq 0$ is final consumption and $h \in[0,1]$ is the sum of market hours and non-market hours:

$$
h=n_{h}+n_{m}
$$

Final consumption is an aggregate over market goods $c_{m}$ and home goods $c_{h}$.

$$
c=\left[\omega_{2} c_{m}^{1-\frac{1}{\xi_{2}}}+\left(1-\omega_{2}\right) c_{h}^{1-\frac{1}{\xi_{2}}}\right]^{\frac{1}{1-\frac{1}{\xi_{2}}}}
$$

Home goods is an aggregate over home capital $k_{h}$ and non market hours $n_{h}$.

$$
c_{h}=\left[\omega_{1} k_{h}^{1-\frac{1}{\xi_{1}}}+\left(1-\omega_{1}\right) n_{h}^{1-\frac{1}{\xi_{1}}}\right]^{\frac{1}{1-\frac{1}{\xi_{1}}}}
$$

. Let us define the expenditure on home capital as $d, d=k_{h} / A_{h}$ and we can rewrite $c_{h}$ as:

$$
c_{h}=\left[\omega_{1}\left(A_{h} d\right)^{1-\frac{1}{\xi_{1}}}+\left(1-\omega_{1}\right) n_{h}^{1-\frac{1}{\xi_{1}}}\right]^{\frac{1}{1-\frac{1}{\xi_{1}}}}
$$

## Household Problem: Labor Productivity

Agents are born with identical preference at age $j=1$ :

$$
\begin{equation*}
\mathbb{E}\left[\sum_{j=1}^{J} \beta^{j}\left(\prod_{m=1}^{m=j} s_{m}\right) u\left(c_{j}, n_{j}\right)\right] \tag{1}
\end{equation*}
$$

Agent's efficiency units per hour of market work (or individual labor productivity) depends on age(experience) and an idiosyncratic component labor productivity $y_{i j}$ that follows the following stochastic process. Therefore, the hourly wage for an individual $i$ of age $j$ is:

$$
\begin{equation*}
p_{i j}=\underbrace{w}_{\text {common wage rate }} \times \underbrace{\exp \left[L(j)+y_{i j}\right]}_{\text {individual i's efficiency unit }} \times \underbrace{\frac{1}{\int_{\mathcal{S}} \exp \left[L(j)+y_{i j}\right] d \lambda}}_{\text {normalization term }} \tag{2}
\end{equation*}
$$

We model $y_{i j}$ as the sum of two orthogonal components: a persistent component $z_{i j} \in \mathcal{Z}$ and a transitory component $\varepsilon_{i j} \in \mathcal{E}$. The initial value of persistent component $z_{i 1}$ is drawn from a initial dispersion that describes the labor productivity differentials when individuals enter into the labor market.

$$
\begin{gather*}
y_{i j}=z_{i j}+\varepsilon_{i j} \\
z_{i j}=\rho z_{i, j-1}+\eta_{i j}  \tag{3}\\
\varepsilon_{i j} \sim N\left(0, \sigma_{\varepsilon}^{2}\right), \quad \eta_{i j} \sim N\left(0, \sigma_{\eta}^{2}\right), \quad z_{i 1} \sim N\left(0, \sigma_{z}^{2}\right)
\end{gather*}
$$

## Bellman Equations

Working age individuals with age $j \in\left\{1,2, . ., J^{w}\right\}$, borrow and save in one period risk free asset. $\tau^{p}$ is public pension fund contribution rate:

$$
\begin{gather*}
V(a, z, j, \varepsilon)=\max _{c_{m}, a^{\prime}, n_{h}, n_{m}, d} u(c, h)+\beta s_{j+1} \mathbb{E}\left[V\left(a^{\prime}, z^{\prime}, j+1, \varepsilon^{\prime} \mid z\right)\right] \quad \text { s.t. }  \tag{4}\\
c_{m}+a^{\prime}+d=\frac{1+r}{s_{j}} a+\left(1-\tau^{p}\right) p(w, z, j, \varepsilon) n_{m} \\
a^{\prime} \geq \underline{a}, c \geq 0, h \in[0,1]
\end{gather*}
$$

For individuals with age $j \in\left\{J^{w}+1, \ldots, J\right\}$, they get retired A fixed amount pension comes from social security fund $b$ will be provided in each period.

$$
\begin{gather*}
V(a, z, j, \varepsilon)=\max _{c, a^{\prime}, n_{h}, d} u(c, h)+\beta s_{j+1} \mathbb{E}\left[V\left(a^{\prime}, z^{\prime}, j+1, \varepsilon^{\prime} \mid z\right)\right] \quad \text { s.t. }  \tag{5}\\
\qquad c+a^{\prime}+d=\frac{1+r}{s_{j}} a+b \\
a^{\prime} \geq \underline{a}, c \geq 0, h=0
\end{gather*}
$$

## Firms and Government

There exists a representative firm who use aggregate capital and labor to produce final good. Firm's output is subject to a value added $\operatorname{tax} \tau^{f}$. Given prices $\{w, r\}$ and tax rate, firms choose input to maximize profit.

$$
\begin{equation*}
\max _{K, H}\left(1-\tau^{f}\right) A K^{\alpha} H^{1-\alpha}-w H-(r+\delta) K \tag{6}
\end{equation*}
$$

The optimality conditions are:

$$
\begin{equation*}
w=(1-\alpha)\left(1-\tau^{f}\right) A K^{\alpha} H^{-\alpha}, \quad r+\delta=\alpha\left(1-\tau^{f}\right) A K^{\alpha-1} H^{1-\alpha} \tag{7}
\end{equation*}
$$

Government has two independent budgets to balance. Pension system is Pay-as-you-go. A system in which retirement benefits are financed by contributions levied from current workers, as opposed to a funded system in which contributions are invested to pay for future benefits. Let $\tau^{b}$ be the replacement rate which measures the ratio of pension benefit to average labor earning for working age population. The pension system budget is:

$$
\begin{equation*}
\tau^{p} w H=b \sum_{j=j^{w}+1}^{J} \mu_{j}=\tau^{b} \frac{w H}{\sum_{j=1}^{J w} \mu_{j}} \sum_{j=j^{w}+1}^{J} \mu_{j} \tag{8}
\end{equation*}
$$

Government expenditure is financed by value added tax.

$$
\begin{equation*}
\tau^{f} A K^{\alpha} H^{1-\alpha}=G \tag{9}
\end{equation*}
$$

## Definition of Recursive Competitive Equilibrium

The state space is denoted by $\mathcal{S} \equiv \mathcal{J} \times \mathcal{A} \times \mathcal{E} \times \mathcal{Z}$. Denote the stationary distribution as $\lambda$.
A competitive equilibrium is a value function $V(s)$; decision rules $c(s), a^{\prime}(s), h(s)$; firm choices $H, K$; prices $r$, $w$, tax rates $\tau^{p}, \tau^{f}$, retirement benefit b government expenditure $G$ and and measures of agents $\lambda$, such that:
(1) Given prices, retirement benefit and tax rates, the policy functions $c(s), a^{\prime}(s), n_{m}(s), n_{h}(s), d$ solve the household's problem (4), (5) for working periods and retirement periods while $V(s)$ is the associated value function.Given prices, the firm chooses optimally its capital K and its labor H , equation (7) is satisfied.Labor market clears.

$$
H=\int_{\mathcal{S}} n_{m}(s) d \lambda
$$Capital market clears. Government budget balances.

$$
K(1+n)=\int_{\mathcal{S}} a^{\prime}(s) d \lambda
$$

(5) Goods market clears

$$
A K^{\alpha} H^{1-\alpha}=\int_{\mathcal{S}} c_{m}(s) d \lambda+(1+n) K-(1-\delta) K+G+\int_{\mathcal{S}} d(s) d \lambda
$$

(6) The government budget is balanced, equation (8), (9) are satisfied.
(7) The invariant distribution $\lambda$ is consistent with household decision rules. For all $s \in \mathcal{S}$ and $\mathbb{S} \in \Sigma_{\mathcal{S}}$, the invariant probability measure $\lambda$ satisfies

$$
\lambda(\mathbb{S})=\int_{\mathcal{S}} Q(s, \mathbb{S}) d \lambda
$$

while the transition function $Q(s, \mathbb{S})$ is defined as: $Q(s, \mathbb{S})=I\{j+1 \in \mathbb{J}\} I\{a(s) \in \mathbb{A}\} \operatorname{Pr}(\varepsilon \in \mathbb{E}) \sum_{z^{\prime} \in \mathbb{Z}} \pi\left(z^{\prime}, z\right)$

## Calibration and Quantification

## Road Map

Calibration

- Externally calibrated parameters
- Time-invariant internally calibrated parameters to match a group of moments in 2010
- Time-varying internally calibrated parameters to match a group of moments in 2020

Main Exercises: compute model simulated moments in two steady states.

- market hours
- non market hours
- correlation between market hours and wage rates

Examine aggregate performance and partial effect from various mechanisms.
Target to match dynamics of two moments

- Average market hours per worker
- Correlation between market hours and wage rates


## First-Stage Calibration

| Parameters | Description/Sources | Value |
| :--- | :--- | :--- |
| Invariant Parameters: | Micro-estimates of intertemporal elasticity of substitution | 1.5 |
| $\gamma$ | Micro-estimates of elasticity of labor supply | 1 |
| $\sigma$ | Length of life cycle age 20-90 | 70 |
| $J$ | Length of working periods age 20-60 | 40 |
| $J^{w}$ | Experience profile from equation | Equation 10 |
| $L(j)$ | Basic old-age insurance public fund tax rate | 0.2 |
| $\tau^{p}$ | No borrowing | 0 |
| $a$ | Capital share | 0.4 |
| $\alpha$ | Capital depreciation rate | 0.05 |
| $\delta$ | Permanent shock | 1 |
| $\rho$ | Government expenditure to GDP ratio | 0.25 |
| $\tau_{f}$ | Normalization | 1 |
| $A^{2010}$ | Normalization | 1 |
| $A_{h}^{2010}$ |  |  |
| Variant $P a r a m e t e r s: ~$ | Wage rate residuals dynamics from CFPS | $0.155 / 0.143$ |
| $\sigma_{\varepsilon, 2010} / \sigma_{\varepsilon, 2020}$ | Wage rate residuals dynamics from CFPS | $0.0076 / 0.0182$ |
| $\sigma_{\eta, 2010} / \sigma_{\eta, 2020}$ | Wage rate residuals dynamics from CFPS | $0.1628 / 0.2400$ |
| $\sigma_{z, 2010} / \sigma_{z, 2020}$ | Age specific survival rate | Figure ?? Panel A |
| $s_{j, 2010} / s_{j, 2020}$ | Growth rate in birth rate | $0 /-0.03$ |
| $n_{2010} / n_{2020}$ |  |  |

## Income Process Estimation: Method

We utilize residuals in hourly wage rate dynamics from CFPS data estimating income process estimation that follows the model. Let $w_{i, j, t}$ be the hourly wage rate for individual $i$, at age $j$ and year $t$. We get residuals by regressing $w_{i, j, t}$ on a time dummy and and a cubic polynomial in potential experience (age minus years of education minus six) $L(j)$.

$$
\begin{equation*}
\ln \left(w_{i, j, t}\right)=\beta_{t}^{0}+L(j)+y_{i, j, t} \tag{10}
\end{equation*}
$$

The specification is consistent with equation (2).Identification is achieved by the following two sets of identities.

$$
\begin{gathered}
\operatorname{Var}\left(y_{i t}\right)-\operatorname{Cov}\left(y_{i, t+2}, y_{i, t}\right)=\sigma_{\varepsilon t}^{2} \\
\operatorname{Var}\left(y_{i t}\right)-\operatorname{Cov}\left(y_{i t}, y_{i, t-2}\right)=\sigma_{\varepsilon t}^{2}+\sigma_{\eta, t-1}^{2}+\sigma_{\eta, t-2}^{2}
\end{gathered}
$$

Variance of initial dispersion is computed as the variance of $\log$ wage in age $j=22$ minus estimated variance of transitory shocks.

$$
\sigma_{z t}^{2}=\operatorname{Var}\left(y_{i, j=22, t}\right)-\sigma_{\varepsilon t}^{2}
$$

## Income Process Estimation: Results

|  | $(1)$ | $(2)$ | $(3)$ |
| :---: | :---: | :---: | :---: |
|  | $\sigma_{\eta}^{2}$ | $\sigma_{\varepsilon}^{2}$ | $\sigma_{z}^{2}$ |
| 2010 |  | 0.125 | 0.1886 |
|  |  | $(0.0123)$ |  |
| 2012 | 0.0066 | 0.185 | 0.1478 |
|  | $(0.0034)$ | $(0.0145)$ |  |
| 2014 | 0.0086 | 0.147 | 0.2016 |
|  | $(0.0044)$ | $(0.0103)$ |  |
| 2016 | 0.0265 | 0.149 | 0.2177 |
|  | $(0.0078)$ | $(0.0085)$ |  |
| 2018 | 0.0171 | 0.118 | 0.2435 |
|  | $(0.0040)$ | $(0.0078)$ |  |
| 2020 | 0.0193 | 0.168 | 0.2364 |
|  | $(0.0061)$ | $(0.0132)$ |  |

Notes: We tabulate the estimation results for income process using CFPS sample from 2010 to 2020. Bootstrap standard error in parentheses.

- Variance of persistent shocks increases
- Initial dispersion increases


## Second and Third Stage Calibration

Table: Summary of Internally Calibrated Parameters

| Parameters | Description/Moments to Match | Value | Relative Moments |
| :--- | :--- | :--- | :--- |
| Second-Stage |  |  |  |
| $\omega_{1}$ | Weight on home capital | 0.55 | Average $d / c_{m}$ |
| $\xi_{1}$ | Sub. betw. $n_{h}$ and $k_{h}$ | 1.52 | Elas. of $n_{h}$ to wage rate |
| $\omega_{2}$ | Weight on market goods | 0.48 | Average $n_{m} / n_{h}$ |
| $\xi_{2}$ | Sub. betw. market and home goods | 2.16 | Elas. of $n_{m} / n_{h}$ to wage rate |
| $\psi$ | Disutility of labor | 4.29 | Average total hours |
| $\beta$ | Discounting factor | 0.987 | Average wealth to income ratio |
| Third-Stage |  |  |  |
| $A^{2020}$ | Productivity in producing final goods 2020 | 1.42 | Change in wage rate |
| $A_{h}^{2020}$ | Productivity in producing home capital 2020 | 1.45 | Change in average $n_{m} / n_{h}$ |

## Quantitative Results

|  | $h$ | $n_{m}$ | $n_{h}$ | $\operatorname{Corr}_{p, n_{m}}$ |
| :---: | :---: | :---: | :---: | :---: |
| Panel A: Model versus Data |  |  |  |  |
| 2010 Data | 0.411 | 0.258 | 0.153 | -0.384 |
| 2010 Model | 0.411 | 0.258 | 0.153 | -0.313 |
| 2020 Data | $\begin{gathered} 0.411 \\ (0.0 \%) \end{gathered}$ | $\begin{gathered} 0.301 \\ (16.7 \%) \end{gathered}$ | $\begin{gathered} 0.110 \\ (-28.1 \%) \end{gathered}$ | -0.418 |
| 2020 Model | $\begin{gathered} 0.402 \\ (-2.2 \%) \end{gathered}$ | $\begin{gathered} 0.296 \\ (14.7 \%) \end{gathered}$ | $\begin{gathered} 0.106 \\ (-30.7 \%) \end{gathered}$ | -0.349 |
| Panel B: Model Partial effect |  |  |  |  |
| TFP | $\begin{gathered} 0.364 \\ (-11.5 \%) \end{gathered}$ | $\begin{gathered} 0.235 \\ (-8.9 \%) \end{gathered}$ | $\begin{gathered} 0.129 \\ (-15.7 \%) \end{gathered}$ | -0.249 |
| Productivity in home capital | $\begin{gathered} 0.393 \\ (-3.9 \%) \end{gathered}$ | $\begin{gathered} 0.282 \\ (9.3 \%) \end{gathered}$ | $\begin{gathered} 0.111 \\ (-28.1 \%) \end{gathered}$ | -0.341 |
| Income Process | $\begin{gathered} 0.431 \\ (4.9 \%) \end{gathered}$ | $\begin{gathered} 0.270 \\ (4.4 \%) \end{gathered}$ | $\begin{gathered} 0.161 \\ (5.2 \%) \end{gathered}$ | -0.344 |
| Demographics | $\begin{gathered} 0.448 \\ (8.3 \%) \end{gathered}$ | $\begin{gathered} 0.283 \\ (9.7 \%) \end{gathered}$ | $\begin{gathered} 0.165 \\ (7.8 \%) \end{gathered}$ | -0.347 |

Conclusion

## Conclusion

- We document the secular trend of time allocation among Chinese.
- We find a rise in both wage rate and market hours among wage workers, which is hard to reconcile.
- We build a quantitative HA model to explain the increase in average market hours.
- TFP growth leads to lower total hours
- Capital augmenting productivity growth shifts up ratio of market to non market hours
- Rising income uncertainty and demographic changes increase total hours
- Successfully recover observed trend

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